

$$1 + 1 > 2$$

# Energy and Mass Defects

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IB PHYSICS | ATOMIC PHYSICS

# Unified Atomic Mass Unit

When measuring and reporting the mass of individual atoms and subatomic particles, kilograms are inconveniently large...

The **unified atomic mass unit** is defined as one-twelfth of the mass of an isolated carbon-12 atom

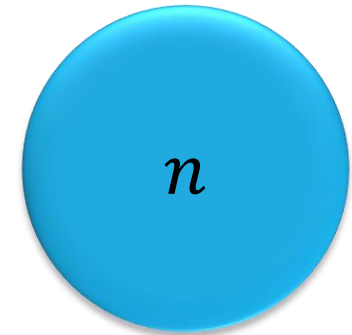
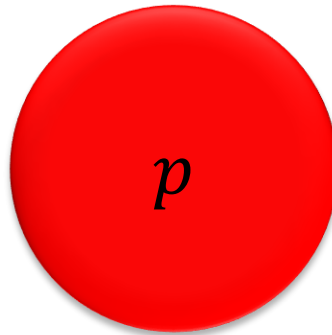
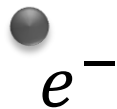
*1 mole of Carbon Atoms = 0.012 kg*

1 u =

# Unified Atomic Mass Unit

Electron ( $m_e$ )	$9.110 \times 10^{-31}$ kg	0.000549 u
Proton ( $m_p$ )	$1.673 \times 10^{-27}$ kg	1.007276 u
Neutron ( $m_n$ )	$1.675 \times 10^{-27}$ kg	1.008665 u
Unified atomic mass unit	$1.661 \times 10^{-27}$ kg	

*This is the only time that we will ever use 7 sig figs. In this case, rounding to 1.01 u just wouldn't cut it...*

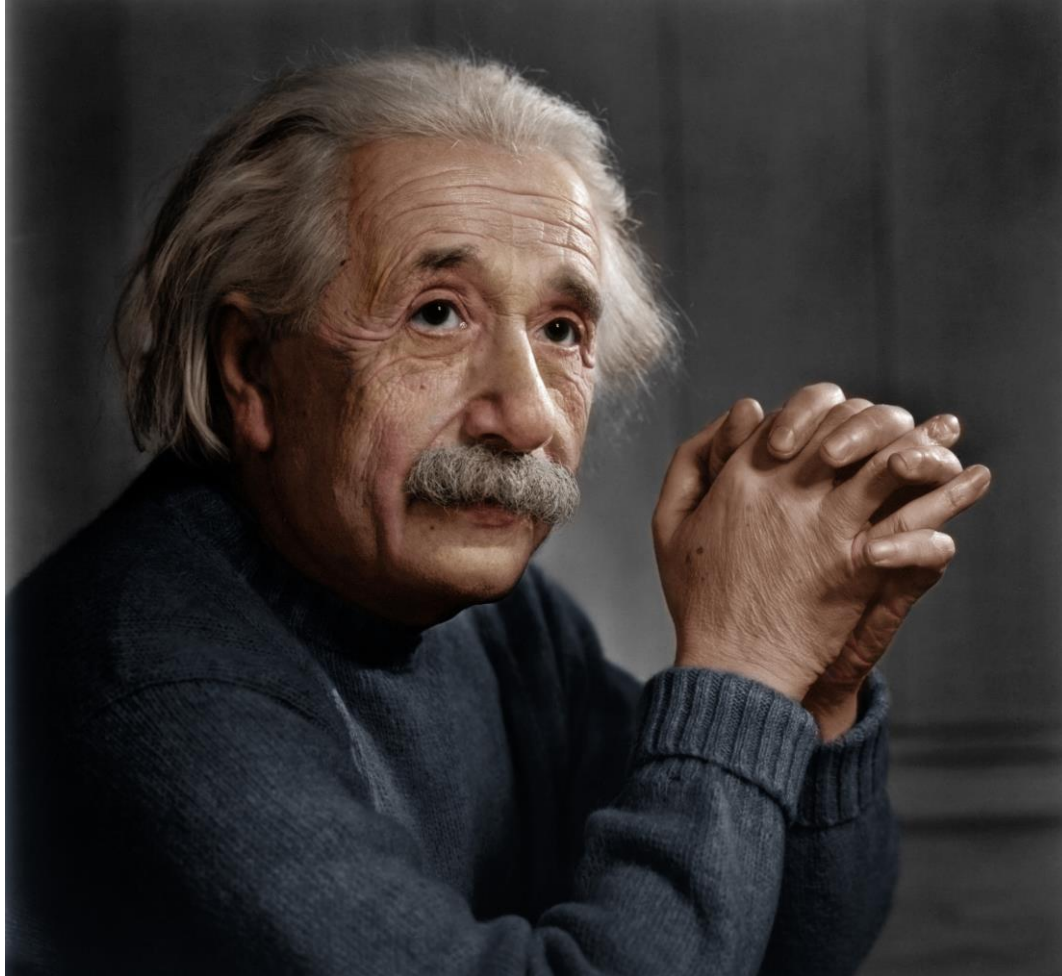


# IB Physics Data Booklet

## Fundamental constants

Quantity	Symbol	Approximate value
Speed of light in vacuum	$c$	$3.00 \times 10^8 \text{ m s}^{-1}$
Planck's constant	$h$	$6.63 \times 10^{-34} \text{ J s}$
Elementary charge	$e$	$1.60 \times 10^{-19} \text{ C}$
Electron rest mass	$m_e$	$9.110 \times 10^{-31} \text{ kg} = 0.000549 \text{ u} = 0.511 \text{ MeV c}^{-2}$
Proton rest mass	$m_p$	$1.673 \times 10^{-27} \text{ kg} = 1.007276 \text{ u} = 938 \text{ MeV c}^{-2}$
Neutron rest mass	$m_n$	$1.675 \times 10^{-27} \text{ kg} = 1.008665 \text{ u} = 940 \text{ MeV c}^{-2}$
Unified atomic mass unit	$u$	$1.661 \times 10^{-27} \text{ kg} = 931.5 \text{ MeV c}^{-2}$
Solar constant	$S$	$1.36 \times 10^3 \text{ W m}^{-2}$
Fermi radius	$R_0$	$1.20 \times 10^{-15} \text{ m}$

# Einstein's Famous Equation



According to Albert Einstein,  
*“mass and energy are  
different manifestations of  
the same things”*

# Einstein's Famous Equation

$$E = mc^2$$

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What is the energy equivalence of 1 g of matter?

# IB Physics Data Booklet

Sub-topic 7.1 – Discrete energy and radioactivity				Sub-topic 7.2 – Nuclear reactions			
$E = hf$ $\lambda = \frac{hc}{E}$				$\Delta E = \Delta m c^2$			
Sub-topic 7.3 – The structure of matter							
Charge		Quarks			Baryon number		
$\frac{2}{3}e$		u	c	t	$\frac{1}{3}$		
$\frac{1}{3}e$		d	s	b	$\frac{1}{3}$		
All quarks have a strangeness number of 0 except the strange quark that has a strangeness number of -1							
Charge		Leptons					
-1		e	$\mu$	$\tau$			
0		$\nu_e$	$\nu_\mu$	$\nu_\tau$			
All leptons have a lepton number of 1 and antileptons have a lepton number of -1							
		Gravitational	Weak	Electromagnetic	Strong		
Particles experiencing		All	Quarks, leptons	Charged	Quarks, gluons		
Particles mediating		Graviton	$W^+, W^-, Z^0$	$\gamma$	Gluons		

$$E = mc^2$$

**YOU MATTER.**

**Until you multiply  
yourself times the speed  
of light squared.  
Then you Energy.**



# New Unit for Energy!

Electron-Volt	eV
1 MeV = $10^6$ eV	

$$\{\textit{Energy in eV}\} = \frac{\{\textit{Energy in J}\}}{1.60 \times 10^{-19}}$$

What is the energy equivalence of 1 proton ( $1.673 \times 10^{-27}$  kg)?

# New Unit for Mass

$$E = mc^2$$



$$m = \frac{E}{c^2}$$

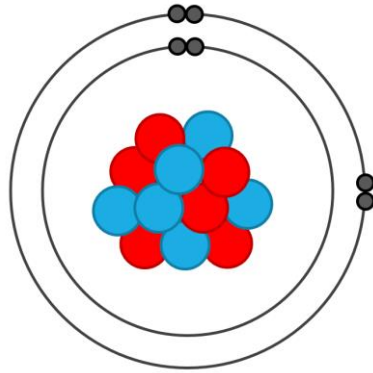
# Unified Atomic Mass Unit

Electron rest mass ( $m_e$ )	$9.110 \times 10^{-31}$ kg	0.000549 u	0.511 MeV $c^{-2}$
Proton rest mass ( $m_p$ )	$1.673 \times 10^{-27}$ kg	1.007276 u	938 MeV $c^{-2}$
Neutron rest mass ( $m_n$ )	$1.675 \times 10^{-27}$ kg	1.008665 u	940 MeV $c^{-2}$
Unified atomic mass unit	$1.661 \times 10^{-27}$ kg	1.000000 u	931.5 MeV $c^{-2}$

# Mass of the Nucleus

A neutral Carbon-12 atom contains:

6 protons  
6 neutrons  
6 electrons



Electron rest mass ( $m_e$ )	0.000549 u
Proton rest mass ( $m_p$ )	1.007276 u
Neutron rest mass ( $m_n$ )	1.008665 u
Unified atomic mass unit	1.000000 u

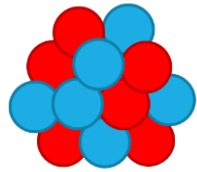
If the mass of Carbon-12 is defined as exactly  $12.000000u$ , then the nucleus mass is:

$$12.000000u - (6 \times 0.000549u) = \mathbf{11.996706u}$$

# Component Mass

A nucleus of Carbon-12 contains:

6 protons  
6 neutrons



What is the total mass in terms of u?

Electron rest mass ( $m_e$ )	0.000549 u
Proton rest mass ( $m_p$ )	1.007276 u
Neutron rest mass ( $m_n$ )	1.008665 u
Unified atomic mass unit	1.000000 u

# Mass Defect | $1+1 > 2$

Mass sum of the Carbon-12 subatomic particles:

$$(6 \times 1.007276\text{u}) + (6 \times 1.008665\text{u}) = 12.095646\text{u}$$

Mass of Carbon-12 nucleus:  $11.996706\text{u}$

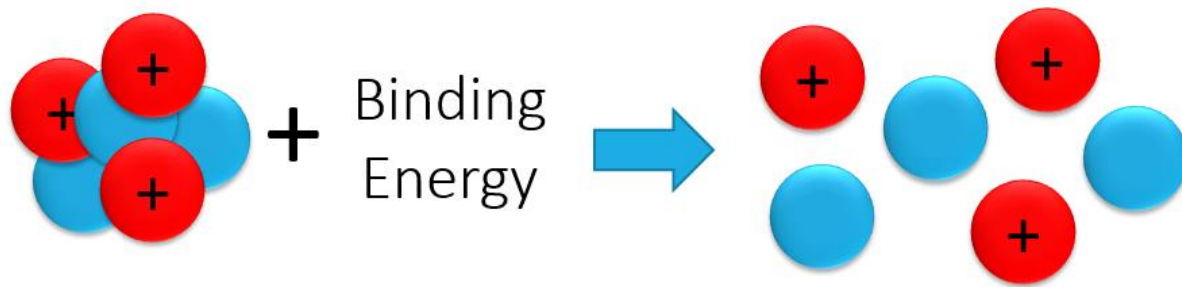
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Mass Defect  $\longrightarrow$   $12.095646\text{u} - 11.99670\text{u} = \mathbf{0.098946\text{u}}$

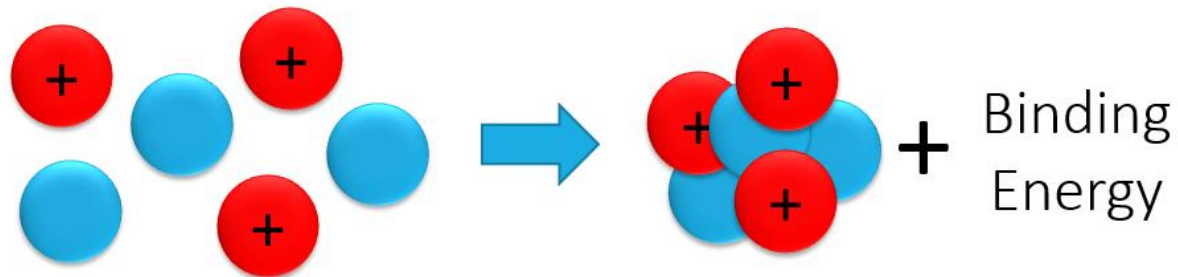
Where did the mass go?

# Binding Energy

Binding Energy is the energy required to separate all of the nucleons



...or the energy released when a nucleus is formed from its nucleons



# Mass Defect → Binding Energy

Unified atomic mass unit	$1.661 \times 10^{-27}$ kg	1.000000 u	931.5 MeV $c^{-2}$
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**0.098946u**

$$E = mc^2$$

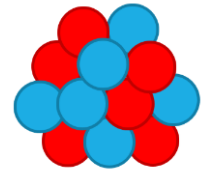


# Binding Energy per Nucleon

Binding Energy for Carbon-12 = 92.2 MeV

Number of Nucleons  
for Carbon-12 =

6 protons  
6 neutrons



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Binding Energy per Nucleon =

# Calculate Binding Energy per Nucleon

Nuclide	# of p	# of n	Nucleus Mass
Iodine-127	53		126.87544u

$m_e$	0.000549u
$m_p$	1.007276u
$m_n$	1.008665u
1u	931.5 MeV $c^{-2}$

# Calculate Binding Energy per Nucleon

\*For your assigned nuclide, calculate the binding energy per Nucleon and record data in shared spreadsheet

Use a periodic table to determine atomic # for your element

$m_e$	0.000549u
$m_p$	1.007276u
$m_n$	1.008665u
1u	931.5 MeV $c^{-2}$

	Element	Nucleus Mass (u)
1	Hydrogen-2	2.013553
2	Helium-3	3.014931
3	Hydrogen-3	3.015500
4	Helium-4	4.001505
5	Lithium-6	6.013476
6	Lithium-7	7.014356
7	Beryllium-9	9.009987
8	Carbon-12	11.996706
9	Nitrogen-14	13.999231
10	Oxygen-16	15.990523
11	Fluorine-19	18.993462
12	Magnesium-24	23.978454
13	Phosphorus-31	30.965527
14	Sulfur-34	33.959083
15	Potassium-39	38.953275

	Element	Nucleus Mass (u)
16	Iron-56	55.920662
17	Arsenic-75	74.903478
18	Krypton-84	83.891734
19	Zirconium-90	89.882739
20	Silver-107	106.879287
21	Tin-120	119.874752
22	Iodine-127	126.875373
23	Cesium-140	139.873608
24	Europium-153	152.886650
25	Tungsten-184	183.910307
26	Gold-197	196.923199
27	Lead-206	205.929447
28	Bismuth-209	208.934833
29	Uranium-235	234.993420
30	Uranium-238	238.000282

# Blank Slide for Calculations 😊