## Circular Motion

## IB Physics Content Guide

## Big Ideas

- Objects moving in a circle are experiencing acceleration since the direction of the velocity is constantly changing
- Centripetal acceleration and centripetal force are always directed toward the center of the circle
- The net force for a body in circular motion is equal to the centripetal force
- It is useful to draw a free body diagram to determine what forces are present at a given position


## Content Objectives

## 1 - Defining Circular Motion

| I can convert between angular displacement in revolutions and radians |  |  |
| :--- | :--- | :--- |
| I can describe and calculate the properties of period and frequency |  |  |
| I can calculate angular velocity |  |  |
| I can describe and calculate tangential velocity based on the angular velocity and radius |  |  |
| I can determine the direction and magnitude of centripetal acceleration and centripetal force |  |  |

## 2 - Vertical Circular Motion

| I can draw correctly proportioned free body diagrams for horizontal and vertical circular motion |  |  |
| :--- | :--- | :--- |
| I can compare the forces on an object at different positions in vertical circular motion |  |  |
| I can identify the combination of forces that make up the net force that results in circular motion. |  |  |
| I can determine the magnitude and direction of the forces needed to move in a vertical circle |  |  |

## 3 - Circular Motion, Friction, and Angles

| I can draw a free body diagram when circular motion is produced by a reaction or friction force |  |  |
| :--- | :--- | :--- |
| I can solve problems that involve friction to create circular motion |  |  |
| I can solve circular motion problems that incorporate components of an angled force |  |  |

## Circular Motion

|  | Variable <br> Symbol | Unit |
| :---: | :---: | :---: |
| Distance | d | m |
| Angular Distance | $\theta$ | rad |
| Angular Velocity | $\omega$ | $\mathrm{rad} \mathrm{s}^{-1}$ |
| Linear Velocity | V | $\mathrm{m} \mathrm{s}^{-1}$ |
| Centripetal Acceleration | $a$ | $\mathrm{~m} \mathrm{~s}^{-2}$ |
| Centripetal Force | $\mathrm{F}_{\mathrm{c}}$ | N |

Shelving Guide
Draw in
vectors
for $v_{,} a_{c}$
and $F_{c} \rightarrow$


Data Booklet Equations:

$$
v=\omega r
$$

$$
a=\frac{v^{2}}{r}=\frac{4 \pi^{2} r}{T^{2}}
$$

$$
F=\frac{m v^{2}}{r}=m \omega^{2} r
$$

## Defining Circular Motion

| $\underbrace{}_{2 \pi \mathrm{rad}}$ | Period | T | s | Angular Velocity | $\omega$ | $\mathrm{rad} \mathrm{s}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Time per revolution |  | $\omega=\frac{2 \pi}{T}$ |  |  |  |

Vertical Circular Motion

|  | Bottom: |
| :--- | :--- | :--- |
| $F_{\text {net }}=F_{C}=F_{T}+F_{g}$ | $F_{\text {net }}=F_{C}=F_{T}-F_{g}$ |

Top: $\quad$ Bottom:

Circular Motion with Friction and Angles


Relationships between variables:

$$
\begin{aligned}
F_{f} & =F_{g} \\
F_{c} & =R
\end{aligned}
$$

| - ${ }^{2}$ |  | Relationships between variables: |
| :---: | :---: | :---: |
|  |  | $R=F_{g}$ |
|  | $\underset{F_{\mathrm{g}}=\mathrm{mg}}{\square}$ | $F_{C}=F_{f}$ |




Relationships between variables:

$$
\begin{aligned}
T_{y} & =F_{g} \\
F_{c} & =T_{x}
\end{aligned}
$$

