## Circuit Analysis

IB PHYSICS | ELECTRICITY

## Review of Parallel Circuits

- Separate branches
- Current splits up between the different pathways
is Junctions is



## Kirchhoff's First Law

The total current coming into a junction must equal the total current leaving the same junction

3 A

2 A


## Kirchhoff's First Law

## $\Sigma I=0$ (junction)

| Entering Junction | $\rightarrow \bullet$ | Positive |
| :---: | :--- | :---: |
| Exiting Junction | $\bullet \rightarrow$ | Negative |


| $(+5)+(-3)+(-2)=0$ |
| :---: |
| 3 A |

$$
\frac{(+5)+(-9)+(+4)=0}{9 \mathrm{~A}}
$$

5 A

4 A

## IB Physics Data Booklet

| Sub-topic 5.1 - Electric fields | Sub-topic 5.2 - Heating effect of electric currents |
| :---: | :---: |
| $\begin{aligned} & I=\frac{\Delta q}{\Delta t} \\ & F=k \frac{q_{1} q_{2}}{r^{2}} \\ & k=\frac{1}{4 \pi \varepsilon_{0}} \\ & V=\frac{W}{q} \\ & E=\frac{F}{q} \\ & I=n A v q \end{aligned}$ | Kirchhoff's circuit laws: $\begin{aligned} & \quad \Sigma V=0 \text { (loop) } \\ & \quad \Sigma I=0 \text { (junction) } \\ & R=\frac{V}{I} \\ & P=V I=I^{2} R=\frac{V^{2}}{R} \\ & R_{\text {total }}=R_{1}+R_{2}+\cdots \\ & \frac{1}{R_{\text {total }}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\cdots \\ & \rho=\frac{R A}{L} \end{aligned}$ |
| Sub-topic 5.3 - Electric cells | Sub-topic 5.4 - Magnetic effects of electric currents |
| $\varepsilon=I(R+r)$ | $\begin{aligned} & F=q v B \sin \theta \\ & F=B I L \sin \theta \end{aligned}$ |

## Find the Missing Currents



## Follow the Current...



## Review of the Water Flow Model



## Each resistor has a "voltage drop"

The voltage used by the resistors equals the voltage supplied by the battery


## Kirchhoff's Second Law

The sum of the voltages (potential differences) provided must equal the voltages dissipated across components

$$
\Sigma V=0(\text { loop })
$$

Across Batteries

| Negative to Positive | $\rightarrow-1$ | Positive |
| :---: | :---: | :---: |
| Oositive to Negative | $\rightarrow \mid$ | Over Resistors: |
| Pogative | Always Negative |  |



$$
(+12)+\underset{\text { Resistor }}{(-4)}+(-8)=0
$$

## Kirchhoff's Second Law

## Across Batteries

## $\Sigma V=0$ (loop)

| Negative to Positive | $\rightarrow-\mid$ | Positive |
| :--- | :--- | :---: |
| Positive to Negative | $\rightarrow-\vdash$ | Over Resistors: |

$$
(+12)+\underset{\text { Resistor }}{(-2)}+(-9)+(-1)=0
$$



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## The Tools for your Toolbox ©

Ohm's Law: If you know two of the three electrical properties: $V$, $I$, or $R$

$$
R=\frac{V}{I}
$$

Kirchhoff's Voltage Law

$$
\Sigma V=0(\text { loop })
$$

Kirchhoff's Current Law
$\Sigma I=0$ (junction)
Series Combination

$$
R_{\text {total }}=R_{1}+R_{2}+\cdots
$$

Parallel Combination

$$
\frac{1}{R_{\text {total }}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\cdots
$$

## Calculating Circuits - Series

No Junction: Current is the same throughout


Loop: Voltage supplied equals voltage dissipated

|  | V | I | R |
| :---: | :---: | :---: | :---: |
| $\mathrm{R}_{1}$ | 2 V | 2 A | $1 \Omega$ |
| $\mathrm{R}_{2}$ | 6 V | 2 A | $3 \Omega$ |
| $\mathbf{R}_{3}$ | 4 V | 2 A | $2 \Omega$ |

## Total <br> 12 V 2 A <br> $6 \Omega$

$$
R_{T}=1+3+2=6 \Omega \quad I_{T}=\frac{V}{R}=\frac{12}{6}=2 \mathrm{~A}
$$

## Calculating Circuits - Parallel



Loop: Voltage supplied equals voltage dissipated Junction: Current in = Current out

|  | V | I | $\mathbf{R}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{R}_{1}$ | 12 V | 2 A | $6 \Omega$ |
| $\mathbf{R}_{2}$ | 12 V | 4 A | $3 \Omega$ |
| Total | 12 V | 6 A | $2 \Omega$ |

$$
\begin{aligned}
& R_{T}=\left(6^{-1}+3^{-1}\right)^{-1}=2 \Omega \\
& I_{T}=\frac{V}{R}=\frac{12}{2}=6 \mathrm{~A} \quad I=\frac{V}{R}=
\end{aligned}
$$

## Patterns



## Series Circuit

- Voltage is divided between components
- Current is the same for all components


## Parallel Circuit

- Voltage is the same for each branch
- Current splits at each junction


## Lesson Takeaways

$\square$ I can use Kirchhoff's First Law to determine an unknown current at a junction
$\square$ I can use Kirchhoff's Second Law to determine an unknown voltage drop in a loop
$\square$ I can calculate voltage, current, and resistance for every component in a simple series or parallel circuit
$\square$ I can compare and contrast the properties for simple series and parallel circuits

