## Impulse \& Momentum Calculations

IB PHYSICS | ENERGY \& MOMENTUM

## Impulse Review

Work $\rightarrow$ Change in Energy
Impulse $\rightarrow$ Change in Momentum

Impulse $=F \Delta t=\Delta p$

## Impulse Slowing Down



Short Time
Large Force
$F \times \Delta t$

Same Mass
Same Momentum

Long Time
Small Force
Long Time
Small Force
Same Impulse


## Impulse Speeding Up

## Impulse $=F \Delta t=\Delta p=m \Delta v$



Same Force
Same Mass


More Time $\rightarrow$ More Velocity

## Slapshot!

A hockey puck has a mass of 0.115 kg . A player takes a slap shot which exerts a force of 31.0 N for 0.15 sec . How fast will the puck be moving?


Initial Momentum $=0 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$
Impulse $=\mathrm{F} \Delta \mathrm{t}=(31 \mathrm{~N})(0.15 \mathrm{~s})=4.65 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$
Final Momentum $=4.65 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}=\mathrm{mv}=(0.115 \mathrm{~kg}) \mathrm{v}$
Final Velocity $=\mathrm{v}=\mathbf{4 0 . 4} \mathrm{m} \mathrm{s}^{-1}$

## Impulse and Momentum

The 440 newton Liquid Apogee Motor (LAM) of India's Mars Orbiter Spacecraft, was successfully fired for a duration of 3.968 seconds on September 22, 2014. This operation of the spacecraft's main liquid engine was also used for the spacecraft's trajectory correction and changed its velocity by $2.18 \mathrm{~m} \mathrm{~s}^{-1}$. What was the mass of the spacecraft at the time of this engine firing?

| Initial |
| :---: | :---: |
| Momentum |$\rightarrow$| Final |
| :---: |
| Momentum |$\quad$| Impulse Added $=F \Delta t=\Delta p$ |
| :--- |

Impulse $=\mathrm{F} \Delta \mathrm{t}=(440 \mathrm{~N})(3.968 \mathrm{~s})=1746 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$
Change in Momentum $=1746 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}=(\mathrm{m})(\Delta \mathrm{v})$

$$
\begin{aligned}
& 1746 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}=(\mathrm{m})(2.18) \\
& \quad \mathbf{m}=\mathbf{8 0 1} \mathbf{~ k g}
\end{aligned}
$$



## Direction Matters



Assume $u$ is $30 \mathrm{~m} \mathrm{~s}^{-1}$ to the left and $v$ is $10 \mathrm{~m} \mathrm{~s}^{-1}$ to the right. What is the change in velocity?

Change in Velocity $=40 \mathrm{~m} \mathrm{~s}^{-1}$

## Try This...

A 500 g baseball moves to the left at $20 \mathrm{~m} \mathrm{~s}^{-1}$ striking a bat. The bat is in contact with the ball for 0.002 s , and it leaves in the opposite direction at $40 \mathrm{~m} \mathrm{~s}^{-1}$. What was average force on ball?

## Initial Momentum <br> $$
\begin{aligned} & p=(0.5)(-20) \\ & -10 \mathrm{~kg} \mathrm{~m} \mathrm{~s} \end{aligned}
$$ <br> Impulse <br> Added <br> $\Delta p$ <br> $30 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$

## Impulse from a Graph



## Try This...

Kara Less was applying her makeup when she drove into South's busy parking lot last Friday morning. Unaware that Lisa Ford was stopped in her lane, Kara rear-ended Lisa's rental car. Kara's 1300-kg car was moving at $5 \mathrm{~m} \mathrm{~s}^{-1}$ and stopped in 0.4 seconds. What was the force?

| Initial <br> Momentum | Impulse |
| :---: | :---: |
| Decreases Momentum |  | | Final |
| :---: |
| Momentum |

Initial Momentum $=m v=(1,300)(5)=6,500 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$
Final Momentum $=0 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$

Impulse $=6,500 \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}=(\mathrm{F})(0.4 \mathrm{~s})$

## Force $=F=16,250 \mathrm{~N}$

## Lesson Takeaways

$\square$ I can use impulse and momentum to solve for an unknown force
$\square$ I can use impulse and momentum to solve for an unknown velocity
$\square$ I can calculate the change in velocity when there is a direction change
$\square$ I can calculate change in momentum from a Force vs Time graph

