ENERGY & MOMENTUM

IB PHYSICS | COMPLETED NOTES

Calculating Energy

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Energy Calculations

Sub-topic 2.3 – Work, energy and power $W = Fs \cos\theta$ $E_{\rm K} = \frac{1}{2}mv^2$ **Kinetic Energy (KE)** $E_{\rm P} = \frac{1}{2} k \Delta x^2$ $\Delta E_{\rm P} = mg\Delta h$ **Potential Energy (PE)** power = Fvuseful work out Efficiency = total work in useful power out = total power in

Who has more energy??



= (100)(9.81)(3)= 2943 J

PE = mgh



 $KE = \frac{1}{2}mv^2$ $=\frac{1}{2}(100)(7.67)^2$ = 2941 J

Understanding Relationships



How does PE change when you triple the height?

3 times PE

How does KE change when you triple the velocity?



Conservation of Mechanical Energy



Conservation of Energy



Conservation of Energy

A 2-kg ball is released from a height of 20 m. What is its velocity when its height has decreased to 5 m?

PE + KE = PE + KE $mgh = mgh + \frac{1}{2}mv^{2}$ $(2)(9.81)(20) = (2)(9.81)(5) + \frac{1}{2}(2)v^{2}$ $392.4 = 98.1 + v^{2}$ v = 17.2 m/s



Try this

The height of the building Spider-Man (a.k.a. Peter Parker, a.k.a. Tobey McGuire) starts off on is 6 stories, or 18 meters high. The height of the building he wants to swing to is 1 story, or 3 meters high. Tobey McGuire is has a mass of approximately 72 kg. Use conservation of energy to calculate his speed when his feet touch the roof of the second building

PE + KE = PE + KE $mgh = mgh + \frac{1}{2}mv^{2}$ $(72)(9.81)(18) = (72)(9.81)(3) + \frac{1}{2}(72)v^{2}$ $12,714 = 2,119 + 36v^{2}$



$$v = 17.2 \text{ m/s}$$

Notice any similarities??

The final velocity is the same in each example. Same height change, mass doesn't matter!

Conservation of Energy

A 2-kg ball is released from a height of 20 m. What is its velocity when its height has decreased to 5 m?

$$PE + KE = PE + KE$$

$$mgh = mgh + \frac{1}{2}mv^{2}$$
(2)(9.81)(20) = (2)(9.81)(5) + $\frac{1}{2}$ (2) v^{2}

$$392.4 = 98.1 + v^{2}$$

$$v = 17.2 \text{ m/s}$$



Try this

The height of the building Spider-Man (a.k.a. Peter Parker, a.k.a. Tobey McGuire) starts off on is 6 stories, or 18 meters high. The height of the building he wants to swing to is 1 story, or 3 meters high. Tobey McGuire is has a mass of approximately 72 kg. Use conservation of energy to calculate his speed when his feet touch the roof of the second building

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v = 17.2 m/s

Try this

What is the velocity of a marble at point A?

*if you aren't given the mass, you should write out the equation and the mass will cancel

Initial Energy = Final Energy PE + KE = PE + KE $mgh = mgh + \frac{1}{2}mv^2$ $(9.81)(100) = (9.81)(70) + \frac{1}{2}v^2$ v = 24.3 m/s



No Mass? No Problem...

Water at the bottom of a waterfall has a velocity of 30 m/s after falling 16 meters. What is the water speed at the top?

PE + KE = PE + KE

$$\frac{1}{2}mv^2 + mgh = \frac{1}{2}mv^2$$
$$\frac{1}{2}v^2 + (9.81)(16) = \frac{1}{2}(30)^2$$

$$v = 24.2 \text{ m/s}$$



Lesson Takeaways

- □ I can describe and calculate kinetic energy and gravitational potential energy
- I can explain the implications of the conservation of energy and show that the total energy in a closed system is always the same
- □ I can interpret a scenario and set up an equality based on the energies present at different locations
- □ I can use the conservation of energy to solve for an unknown energy or variable in a problem

Work and Power

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Where did the energy come from?



Where did the energy come from?

Initial Energy | Final Energy **0** J $\frac{1}{2}mv^2 = \frac{1}{2}(200)(5)^2$ **2500** J





Let's give it a name

When the energy is added to or removed from a system, we call it

Work

How does Science Define Work?

Work is done when a **force** is applied to an object and the object moves in the same direction as the applied force.

How do you Calculate Work

Work* = Force × Displacement

*When force is constant and in the same direction as the movement



The things necessary for Work

- There must be a force
- There must be a displacement

What about direction?

Work at an Angle

Must use the component of the force that is in the same direction as the motion



Work at an Angle



Does this always work?



Try This



When you push a lawn mower, you are really applying a force down the angled handle bar as shown in this picture

How much **work** do you do when you push a lawn mower 20 m with a force of 200 N directed at an angle of 30° with the ground?

$W = Fs \cos\theta = (200)(20)\cos(30^\circ) = 3464 \text{ J}$

Work-Energy Theorem

If energy is truly conserved, how can things ever start or stop moving?

Energy is still conserved (not created or destroyed), it's just being transferred in or out of the system/object that we are studying (gained or lost)



Work as the transfer of energy | Work and energy | Physics | Khan Academy

Work-Energy Theorem

Your engine applies 1000 N of force over a distance of 50 m. If you started from rest and your car has a mass of 2000 kg, how fast are you moving after travelling that distance?



Try This

A 75 kg skateboarder kicks off with an initial velocity of 2 m s⁻¹ and comes to a stop after 15 m. What is the force of friction?



Think about it...

Is a waiter carrying a heavy tray of food at a constant velocity across a room doing any work on the tray?

No, the force is not in the same direction as the displacement



Doesn't change the tray's ENERGY

Think about it...

A particle of mass m is moving with constant speed v in uniform circular motion. What is the total work done by the centripetal force during one revolution?



A.ZeroB.mv²/2

C. mv^2

D. $2\pi mv^2$

Is the earth's gravity doing any work on the moon?

Think about it...

Two physics students, Maria and Paige, are going from the first floor to the second floor on their way to their next class.

- Maria walks up the 3 meter tall staircase in 15 seconds
- Paige runs up the 3 meter tall staircase in 5 seconds

If they both have a mass of 60 kg, which student does the most work?

Same

Work only depends on force and distance



What is Power?

Power is the **rate** at which **work** is done.

(how much work is done in a given amount of time)

How do you Calculate Power

Power = Work / Time



Say Watt?!?

Common Appliances	Estimated Watts
Blender	300-1000
Microwave	1000-2000
Waffle Iron	600-1500
Toaster	800-1500
Hair Dryer	1000-1875
TV 32" LED/LCD	50
TV 42" Plasma	240
Blu-Ray or DVD Player	15
Video Game Console (Xbox / PS4 / Wii)	40-140

We will be looking at power again this year when we discuss electricity...

Lesson Takeaways

- □ I can define and calculate the property of work
- □ I can calculate work when the force is at an angle to the direction of the motion
- I can equate work done on a system to the change in energy of an open system
- I can use the work-energy theorem to solve for an unknown
- I can identify situations where there is motion but no work being done

Elastic Potential Energy

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Calculating from a Graph


Graph of Force vs Displacement



Work of a Varying Force

Our definition of work applies only for a <u>constant</u> force or an <u>average</u> force.

$W = Fs \cos\theta$

What if the force <u>varies</u> with displacement as with stretching a spring or rubber band?



What about a Varying Force?



Click here for the simulation

Work of a Varying Force

How can you calculate the work?



 $Area = \frac{1}{2}(10 \text{ m})(40 \text{ N})$ = 200 J

Work of a Varying Force



Elastic Potential Energy



As the pull back distance increases elastic potential energy <u>increases</u>

Hooke's Law



Try this...

A block with a mass of 2 kg is suspended from a spring and produces the displacement shown. What is the spring constant?

$F = k\Delta x$ (19.62 N) = k(4 m)

$$k = 4.9 \text{ Nm}^{-1}$$



Work and Energy

Work done on a system causes the system to gain or lose energy

Stretching or compressing a spring **stores energy**





Work of a Varying Force

Now that we know that $F = k\Delta x$, we can calculate the stored elastic potential energy with the work equation



Work = Fs $= \left(\frac{1}{2}F\right)s$ $= \left(\frac{1}{2}k\Delta x\right)\Delta x$ Elastic $= \frac{1}{2}k\Delta x^{2}$ Potential

Elastic Force and Work



$$F = k\Delta x$$

$$E_p = \frac{1}{2}k\Delta x^2$$

*The spring constant k is a property of the spring

Data Booklet

Sub-topic 2.3 – Work, energy and power $W = Fs \cos\theta$ $W = FS \cos \theta$ $E_{\rm K} = \frac{1}{2}mv^2 \quad \text{velocity KE}$ $E_{\rm P} = \frac{1}{2}k\Delta x^2 \quad \text{elastic PE}_{\rm e}$ $\Delta E_{\rm P} = mg\Delta h \quad \text{gravity PE}_{\rm g}$ power = Fvuseful work out Efficiency = total work in useful power out = . total power in

Conservation of Energy

How far up the 15° incline of a pinball table will a 0.1 kg pinball move after it is launched? The spring constant is 100 N/m and is compressed by 0.08 m.



 $KE + PE_e + PE_g = KE + PE_e + PE_g$ $\frac{1}{2}k\Delta x^2 = mgh$ $\frac{1}{2}(100)(0.08)^2 = (0.1)(9.81)(h)$

Try this...

What **work** is required to stretch this spring $(k = 200 \text{ N m}^{-1})$ from $\Delta x = 0.1 \text{ m}$ to $\Delta x = 0.4 \text{ m}$?

Initial

$$\frac{1}{2}k\Delta x^{2} = \frac{1}{2}(200)(0.1)^{2} = 1 J$$

$$\frac{1}{2}k\Delta x^{2} = \frac{1}{2}(200)(0.4)^{2} = 16 J$$
Added to the system through work on spring



Try this...

What **work** is required to stretch this spring $(k = 200 \text{ N m}^{-1})$ from $\Delta x = 0.1 \text{ m}$ to $\Delta x = 0.4 \text{ m}$?

Why not just use the stretch change?

1(200)(0)



The force isn't starting at zero!



Example IB Question

An increasing force acts on a metal wire and the wire extends from an initial length I_0 to a new length I. The graph shows the variation of force with length for the wire. The energy required to extend the wire from I_0 to I is E. The wire then contracts to half its original extension. What is the work done by the wire as it contracts?



Lesson Takeaways

- I can calculate work as area bounded by a Force vs Distance graph
- I can use Hooke's Law to calculate the elastic force at a given displacement
- □ I can describe and calculate elastic potential energy



Conservation of Momentum

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What is Momentum??

"Inertia in Motion"



Which has more Momentum??



Which has more Momentum??



Momentum Equation

Momentum = mass × velocity



IB Physics Data Booklet



Conservation of Momentum

The total momentum of a system is constant







"Explosion"

"Hit and Bounce"

"Hit and Stick"

Newton's Third Law

For every action, there is an equal and opposite reaction



Conservation of Momentum



When a cannonball is fired out of a cannon, there is a recoil...

Equal and Opposite...

More mass \rightarrow Less velocity Less mass \rightarrow More velocity

Explosion



Hit and Bounce #1



Before After (8)(10) + (2)(0) = (8)(2) + (2)(v)

80 + 0 = 16 + 2v







Hit and Bounce #2

Before After (12)(8) + (18)(-4) = (12)(-5.5) + (18)(v) 96 + -72 = -66 + 18v







Hit and Stick

Before After (12)(4) + (18)(0) = (30)(v) 96 + 0 = 30v $v = 1.6 \text{ m s}^{-1}$





Elastic vs Inelastic



Inelastic



Kinetic Energy is conserved

Kinetic Energy is <u>not</u> conserved

In both cases momentum is ALWAYS conserved



Try This...



A toy railcar of mass 2 kg travelling at 6 m s⁻¹ collides with another railcar of mass 3 kg travelling at 4 m s⁻¹ in the same direction. If after the collision the two trucks become joined together, what is their resulting velocity?

Before After (2)(6) + (3)(4) = (2 + 3)(v)12 + 12 = 5v

$$v = 4.8 \, m \, s^{-1}$$

Compare the total Kinetic Energy before and after:



System loses **2.4 J** of Kinetic Energy so it is an inelastic collision

Lesson Takeaways

- □ I can define and calculate momentum
- □ I can use the conservation of momentum to solve for missing variables in linear collisions
- □ I can describe the process required for explosion, hit and bounce, and hit and stick scenarios
- I can describe the difference between elastic and nonelastic collisions
- □ I can calculate the amount of energy retained in a nonelastic collision

Impulse

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Remember Work?

Work = Force × Distance



Initial Energy = 0 J

Work = (5,000 N)(100 m) = 500,000 J - Energy added to system

Final Energy = 500,000 J = $\frac{1}{2}$ mv² = $\frac{1}{2}(2,000 \text{ kg})v^2$

Final Velocity = $v = 22.36 \text{ m s}^{-1}$
Introducing Impulse



Initial Momentum = 0 kg m s^{-1}

Impulse = (5,000 N)(8.94 s) = 44,700 kg m s⁻¹ - Momentum added to system

Final Momentum = $44,700 \text{ kg m s}^{-1} = \text{mv} = (2,000 \text{ kg})\text{v}$

Final Velocity = $v = 22.35 \text{ m s}^{-1}$

Impulse

Work \rightarrow Change in Energy Impulse \rightarrow Change in <u>Momentum</u>

What about Units? $[N] = [kg][m s^{-2}]$ Impulse = F × t = $[N][s] = [kg][m s^{-2}][s]$ Impulse = [N s] or $[kg m s^{-1}]^*$

*same unit as momentum

IB Physics Data Booklet



Impulse and Momentum

Impulse can act to increase or decrease an object's momentum

Final Velocity 0 *m/s* Initial Velocity 0 m/s

Initial Velocity 0 m/s







How are these the same? different?





Impulse → Slowing Down



How can we decrease the force acting on an object?



Impulse and Momentum

Impulse = $F\Delta t = \Delta p$



Same Mass Same Momentum Short Time Large Force

 $F \times \Delta t$



E CHA

Same Impulse



Long Time Small Force



Impulse to Speed Up



Should a cannon have a long or short barrel to produce to largest final velocity? Why?

Both designs will experience the same force but the long barrel experiences that force for more time and creates a larger impulse / change in momentum

Marshmallow Shooter



Marshmallow Shooter

Impulse = $F\Delta t = \Delta p = m\Delta v$



Same Force Same Mass





More Time \rightarrow More Velocity

What if the force isn't constant?



Remember how we found work done by a varying force?



Which impulse is larger?



Same Twice the time

Half the force

The force matters!



Increase time to decrease force below a dangerous threshold

F

Lesson Takeaways

- □ I can describe the meaning of impulse and how it is related to momentum change
- □ I can conceptually describe how to decrease the force experienced in a collision
- I can determine the impulse of a collision from a force vs time graph

Impulse & Momentum Calculations

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Impulse Review

Work → Change in Energy Impulse → Change in Momentum

$Impulse = F\Delta t = \Delta p$

Impulse Slowing Down



Short Time Large Force

 $F \times \Delta t$



Same Mass Same Momentum

Same Impulse



Long Time Small Force



Marshmallow Shooter

Impulse = $F\Delta t = \Delta p = m\Delta v$



Same Force Same Mass





More Time \rightarrow More Velocity

Slapshot!

A hockey puck has a mass of 0.115 kg. A player takes a slap shot which exerts a force of 31.0 N for 0.15 sec. How fast will the puck be moving?



Initial
MomentumImpulse AddedFinal
MomentumInitial Momentum = 0 kg m s⁻¹Impulse = $F\Delta t = (31 \text{ N})(0.15 \text{ s}) = 4.65 \text{ kg m s}^{-1}$ Final Momentum = 4.65 kg m s⁻¹ = mv = (0.115 kg)v

Final Velocity = v = **40.4 m s⁻¹**

Impulse and Momentum

The 440 newton Liquid Apogee Motor (LAM) of India's Mars Orbiter Spacecraft, was successfully fired for a duration of 3.968 seconds on September 22, 2014. This operation of the spacecraft's main liquid engine was also used for the spacecraft's trajectory correction and changed its velocity by 2.18 m s⁻¹. What was the mass of the spacecraft at the time of this engine firing?



Impulse = $F\Delta t$ = (440 N)(3.968 s) = 1746 kg m s⁻¹

Change in Momentum = 1746 kg m s⁻¹ = (m)(Δv)

1746 kg m s⁻¹ = (m)(2.18)



Direction Matters



Assume *u* is 30 m s⁻¹ to the left and *v* is 10 m s⁻¹ to the right. What is the change in velocity?

Change in Velocity = 40 m s⁻¹

Try This...

A **500 g** baseball moves to the left at **20 m s⁻¹** striking a bat. The bat is in contact with the ball for **0.002 s**, and it leaves in the opposite direction at **40 m s⁻¹**. What was average force on ball?

 $-10 \text{ kg m s}^{-1} \qquad \Delta p$ 30 kg m s^{-1} 20 m s^{-1} $\text{Impulse} = F\Delta t = \Delta p$ $\text{Impulse} = F(0.002 \text{ s}) = 20 \text{ km m}^{-1}$

p = (0.5)(-20)

m = 0.5 kg

Impulse = $F(0.002 \text{ s}) = 30 \text{ kg m s}^{-1}$

Impulse

Added

F = 15,000 N

p = (0.5)(40)

20 kg m s⁻¹

Impulse from a Graph



Try This...

Kara Less was applying her makeup when she drove into South's busy parking lot last Friday morning. Unaware that Lisa Ford was stopped in her lane, Kara rear-ended Lisa's rental car. Kara's 1300-kg car was moving at 5 m s⁻¹ and stopped in 0.4 seconds. What was the force?



Initial Momentum = $mv = (1,300)(5) = 6,500 \text{ kg m s}^{-1}$

```
Final Momentum = 0 \text{ kg m s}^{-1}
```

Impulse = $6,500 \text{ kg m s}^{-1} = (F)(0.4 \text{ s})$

Force = F = **16,250** N

Lesson Takeaways

- I can use impulse and momentum to solve for an unknown force
- □ I can use impulse and momentum to solve for an unknown **velocity**
- I can calculate the change in velocity when there is a direction change
- I can calculate change in momentum from a Force vs Time graph